

Investigating the Transonic Flutter Boundary of the Benchmark Supercritical Wing

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This paper builds on the computational aeroelastic results published previously and generated in support of the second Aeroelastic Prediction Workshop for the NASA Benchmark Supercritical Wing configuration. The computational results are obtained using FUN3D, an unstructured grid Reynolds-Averaged Navier-Stokes solver developed at the NASA Langley Research Center. The analysis results focus on understanding the dip in the transonic flutter boundary at a single Mach number (0.74), exploring an angle of attack range of -1° to 8° and dynamic pressures from wind off to beyond flutter onset. The rigid analysis results are examined for insights into the behavior of the aeroelastic system. Both static and dynamic aeroelastic simulation results are also examined.

Nomenclature

		α	Angle of attack, degs
c	Wing chord, 16 inches	α_0	Angle of attack, without any aeroelastic influences (rigid, wind off), degs
C_L	Lift coefficient	α_{total}	Total angle of attack, explicitly incorporating aeroelastic influences, degs
$C_{L\alpha}$	Derivative of lift coefficient due to angle of attack	$\bar{\alpha}$	Rigid angle of attack, biased such that $C_{m_0} = 0$, see eqn 7
C_m	Pitching moment coefficient	ω, f	Frequency - radians/second, Hz
$C_{m\alpha}$	Derivative of pitching moment coefficient due to angle of attack	θ	Aeroelastic increment in the pitch angle or angle of attack, degs
C_p	Coefficient of pressure	ζ	Damping ratio
$gvel_0$	Initial perturbation of the generalized velocity	AePW	Aeroelastic Prediction Workshop
K_θ	Stiffness of the pitching degree of freedom	BSCW	Benchmark Supercritical Wing
M	Mach number	CFL	Courant-Freidrichs-Lewy number
\bar{q}	Dynamic pressure, psf	FRF	Frequency Response Function
S	Wing area, 512 inches ²	OTT	Oscillating Turntable
SE	Estimated standard error	PAPA	Pitch and Plunge Apparatus
\bar{x}_{ac}	Aerodynamic center location, in fraction of wing chord, measured positive aft from the leading edge	RANS	Reynolds-Averaged Navier-Stokes
x/c	chordwise location, normalized by chord length	TDT	Transonic Dynamics Tunnel
\bar{x}_{cp}	Center of pressure location, in fraction of wing chord, measured positive aft from the leading edge	TE	Temporal Error

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I. Introduction

Geometric simplicity first drew us to the Benchmark Supercritical Wing (BSCW) as an analysis configuration for the Aeroelastic Prediction Workshop (AePW). With an outer mold line machined from a block of aluminum, the wing itself is one of the most rigid aeroelastic models ever tested in the Transonic Dynamics Tunnel (TDT); the flexibility was provided principally by the TDT Pitch and Plunge Apparatus (PAPA). The PAPA is a two degree-of-freedom (pitch and plunge) sidewall mount system constructed of bars arranged to produce the desired pitch and plunge mode stiffness values, and masses positioned to decouple the wind off modal mass properties. This mount system was engineered by Farmer,¹ who reported experimental results for a supercritical wing showing similar transonic aeroelastic characteristics to the computational results presented in the current paper.

The simplicity of the PAPA structure has allowed us to study the flow field evolution as Mach, angle of attack and excitation level are varied, and the resulting effects on the aeroelastic deformation (static aeroelastic deflection) and stability (flutter). This paper and its companion publication² endeavor to present a sufficient summary of results to show the influences of shock development and separation onset on the aeroelastic characteristics of the BSCW wing. The goal of the work is to develop and understand the bucket in the transonic flutter boundary for this configuration. Historically, the location (in terms of Mach number) and depth (in terms of dynamic pressure or velocity) of the transonic dip have been shown to be functions of the angle of attack. There are many configurations where this behavior has been observed in the technical literature, including both computational and experimental examples. A specific example for the NACA 64 A-010 airfoil is reproduced from reference 3 in Figure 1.

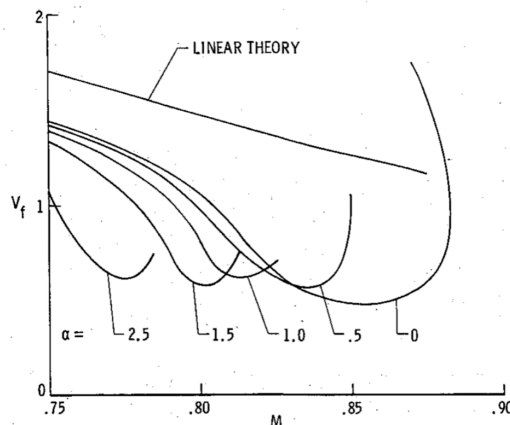


Figure 1. Effect of angle of attack on NACA 64 A-010 flutter boundaries; Source: Reference 3, Figure 7.

While previous publications associated with AePW-2 concentrated on the overall summary of the computational results generated for the workshop,⁴ in this paper, we will be reporting on the predictions from a single code, FUN3D. We focus principally on the influences of the separated flow onset, induced in this study through three effects: angle of attack, dynamic pressure and initial excitation. Only one Mach number is examined—Mach 0.74. Angles of attack from -1° to 8° are examined, with the primary investigations at angles of attack of 0° , 3.15° , 5° and 6.5° . The dynamic pressure ranges examined for each angle of attack begin at the rigid condition and range to above the predicted flutter onset condition. Distributions of steady pressure coefficient for the static rigid BSCW configuration are compared with experimental information over the angle of attack range where that information is available, which ends at 5° . The flutter onset prediction at 0° is compared with the corresponding result from experiment. Unfortunately, the experimental flutter boundary at nonzero angles of attack is not available for a similar comparison at this Mach number. In fact, very little quantitative information is available for any of the conditions where the simulations indicate that separated flow effects dominate the stability.

The paper is organized into five major sections. Background material on the configuration and its uses in the Aeroelastic Prediction Workshops are presented first. The analysis processes are then discussed, followed by results from each of the three analysis processes used here: rigid steady, static aeroelastic and dynamic aeroelastic analyses. The dynamic aeroelastic results include effects of matched point conditions, single degree of freedom representation, perturbation level and spatial resolution. The final two sections contain discussions of continuing analyses and conclusions.

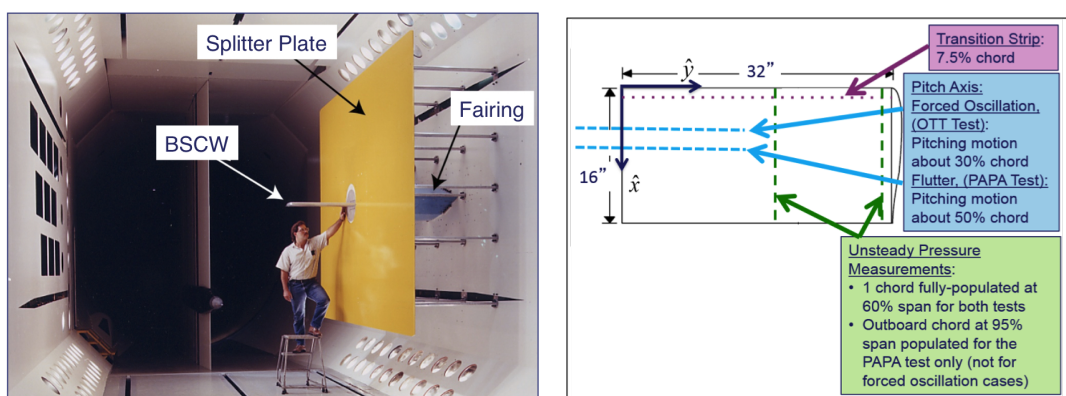
II. Background

A. The BSCW Model and Test Cases

The BSCW model, shown in Figure 2, has a simple, rectangular, 16- x 32-inch wing planform, with a NASA SC(2)-0414 airfoil. It was first tested in the TDT in 1991.⁵ For this test, the wing was mounted on the TDT Pitch and Plunge Apparatus (PAPA) to obtain the flutter boundary at various Mach numbers and angles of attack for this two-degree of freedom system. In 2000, the wing was tested again, this time on an Oscillating Turntable (OTT).⁶ The purpose of the OTT test was to measure aerodynamic response during sinusoidal (forced) pitch oscillation of the wing.

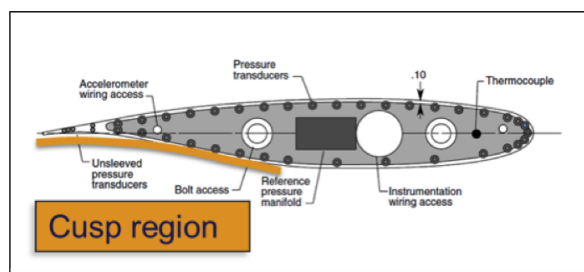
For both the OTT and PAPA tests, the model was mounted to a large splitter plate, sufficiently offset from the wind-tunnel wall (40 inches) to (1) place the wing closer to the tunnel centerline and (2) be outside the tunnel wall boundary layer.⁷ The wing was designed to be rigid, with the following structural frequencies for the combined installed wing and OTT mounting system: 24.1 Hz (spanwise first bending mode), 27.0 Hz (in-plane first bending mode), and 79.9 Hz (first torsion mode). When installed on the PAPA mount, the combined system frequencies were 3.33 Hz for the plunge mode and 5.20 Hz for the pitch mode.⁸ The plunge and pitch modes are the only modes included in the aeroelastic analyses of the PAPA-mounted configuration to be presented in this paper.

For instrumentation, the model has pressure ports in chordwise rows at the 60% and 95% span locations. For the BSCW/PAPA test, both rows were fully populated with unsteady in situ pressure transducers. The quantitative information obtained consists of unsteady data at flutter points and averaged data on a rigidized apparatus at the flutter conditions. For the BSCW/OTT test, only the inboard row at 60% span was populated with transducers. The quantitative information for the OTT test consists of unsteady pressure data and accelerometer data for forced pitch oscillations and for the unforced system at stabilized flow conditions.



(a) Photograph of the BSCW model mounted on the OTT in the TDT.

(b) BSCW geometry.



(c) Cross-sectional view of the SC(2)-0414 airfoil, with BSCW instrumentation.

Figure 2. BSCW model.

B. The First Aeroelastic Prediction Workshop

The first AIAA Aeroelastic Prediction Workshop (AePW-1) took place in conjunction with the AIAA Structural Dynamics and Materials (SDM) conference in April 2012.⁹ This workshop utilized three configurations, including the

BSCW. There were three BSCW test cases for this workshop: a rigid steady analysis and two forced oscillation analyses, all at Mach 0.85, 5° angle of attack. The submitted simulation results for the BSCW contained the most widely varying results of all of the AePW-1 configurations.¹⁰ These variations were observed in the steady results as well as in the frequency response functions. Predictions of the upper surface shock location spanned more than 20 percent of the chord.¹¹ Because of these wide variations, further studies were initiated to understand the underlying causes.

C. The Second Aeroelastic Prediction Workshop

The second AIAA Aeroelastic Prediction Workshop (AePW-2) took place in conjunction with the AIAA SciTech 2016 Conference.⁴ The computational aeroelasticity community was challenged to analyze the BSCW configuration at three conditions (M=0.7 at 3° angle of attack on the OTT; M=0.74 at 0° angle of attack on the PAPA; and M=0.85 at 5° angle of attack on the PAPA) and to present their results at the workshop. The experimental data from the OTT test indicated that the BSCW exhibited a strong shock and boundary-layer-induced separated flow at a moderate angle of attack at transonic conditions.¹² The computations of the transonic flow, in conjunction with the flutter boundary predictions, were therefore the focus of the workshop.¹³ The summary of flutter onset predictions from AePW-2 is shown in Figure 3. The predictions at Mach 0.74, 0° angle of attack have considerably less scatter than the prediction at Mach 0.85, 5° angle of attack. The lower Mach number, lower angle of attack predictions also surround the experimental flutter onset condition, 169 psf.

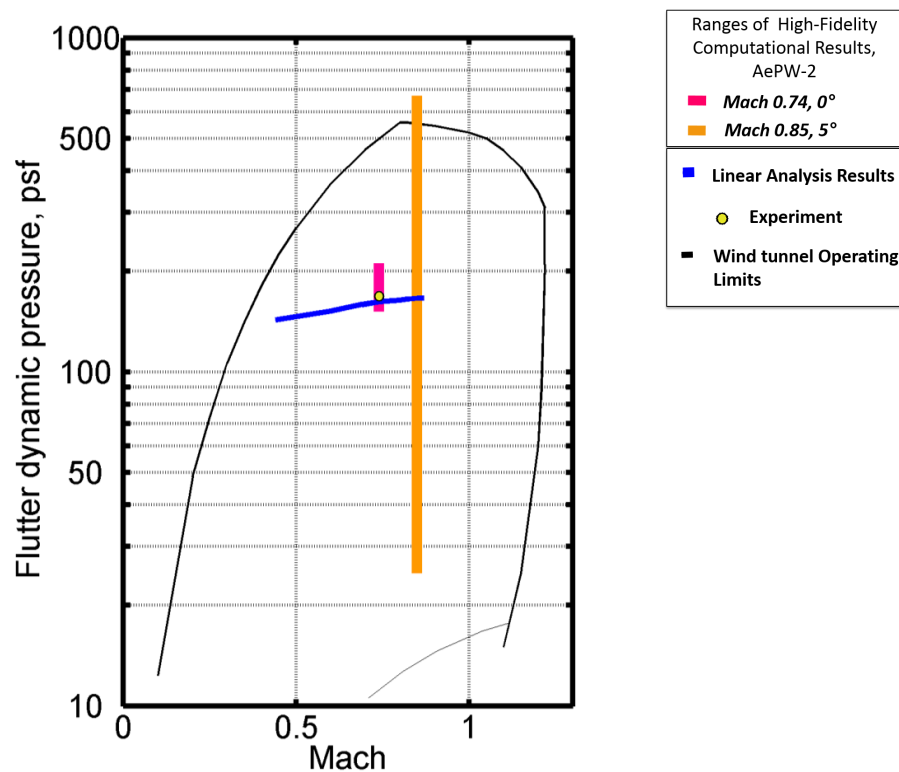


Figure 3. Flutter boundary results from AePW-2.

D. Grids

For the present study, two of the unstructured grids that are detailed in reference 2 were utilized: the designated “medium” grid (9 million nodes) and the designated “Grid D” (35 million nodes). In the current paper, Grid D is referred to as the extra fine grid. The grid distributions for both the wing surface and the plane of symmetry are presented in Figure 4.

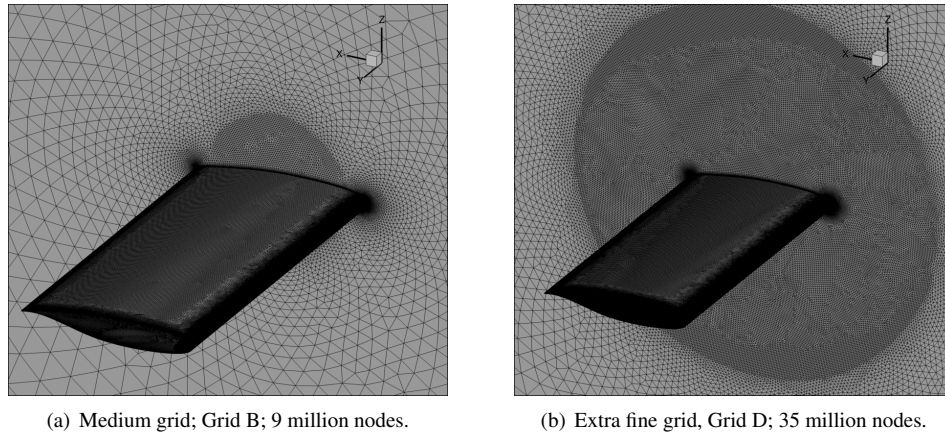


Figure 4. Medium and extra fine grids.

III. Analysis Processes

Solutions to the Reynolds-Averaged Navier-Stokes (RANS) equations were computed using the NASA Langley-developed computational fluid dynamics (CFD) software FUN3D.¹⁴ The flow solutions were produced with turbulence closure obtained using the Spalart-Allmaras (SA) one-equation model.^{15,16} Inviscid fluxes were computed using the Roe scheme,¹⁷ primarily without a flux limiter. The solutions were produced by running three distinct analyses, differentiated by the treatment of the structure, the initial condition and the temporal parameters. The rigid, static aeroelastic and dynamic aeroelastic solution processes are described below.

A. Rigid Analysis

The initial solution for each angle of attack at Mach 0.74 was generated for a rigid wing. In general, these solutions were run in a “steady” mode, in which the solutions computed were not time-accurate and the structure was represented as a fixed position outer mold line. The position (angle) was different for each angle of attack and analyzed in an individual simulation. Time integration was accomplished by an Euler implicit backwards difference scheme, with local time stepping to accelerate convergence. Although some of the cases were not asymptotically steady, the rigid steady simulation was still the first step performed. The cases that were not asymptotically steady occurred at the higher angles of attack and will be identified as a subset of the results presented. These cases did not converge to a fixed pressure distribution and should be run in a time-accurate manner where the range of the physical solution can be established. Results of time-accurate rigid simulations are not presented in the current paper.

B. Unsteady Aeroelastic Analyses

For aeroelastic analyses, the flow equations were solved in a time-accurate mode¹⁸ coupled with a structural solver, allowing the grid to deform. For this work, this coupling was performed internal to the FUN3D code¹⁹ using a modal representation of the structural dynamics. This modal solver was formulated and implemented in FUN3D in a manner similar to other NASA Langley aeroelastic codes (CAP-TSD²⁰ and CFL3D²¹). For the BSCW computations presented here, the structural modes were obtained via normal modes analysis (solution 103) with the Finite Element Model (FEM) solver in MSC NastranTM.²² The modes were then interpolated to the surface mesh using the method developed by Samareh.²³ The BSCW FEM is described in reference 13.

To solve the unsteady flow equations, the FUN3D solver employs a dual-time-stepping method, which is widely used in CFD. This method involves adding a pseudo-time derivative of the conserved variables to the physical time derivative that appears in the Navier-Stokes equations. Subiterations are run within each physical (global) time step to converge the flow solution. Convergence here refers to the process where the pseudo-time derivative vanishes as the subiterations proceed within each physical time step. At the end of the iterative process, a solution to the original unsteady Navier-Stokes equations is obtained for that physical time step. For an infinitely large physical time step, the dual-time solver becomes identical to the steady-state solver, though of course, all time accuracy is lost.

Aeroelastic analysis requires a grid deformation capability. The grid deformation in FUN3D is treated as a linear elasticity problem. In this approach, the grid points near the body can move significantly, while the points farther away

may not move at all. For the aeroelastic simulations in this paper, a predictor-corrector coupling method between the flow solution and the structural solution has been used. Within each physical time step, the flow field solution is converged using the subiterations and subsequently coupled with the structural equations. This coupling occurs only once for each physical time step. The coupling is described further and explored in detail in reference 2.

1. Static Aeroelastic Analysis

The static aeroelastic simulation procedure begins from the last point in the rigid steady solution at identical Mach number and unloaded (rigid) angle of attack. Static aeroelastic simulations are obtained by restarting the CFD analysis from this rigid steady solution. A high value of structural damping (0.9999) is used to allow the structure to find the equilibrium position with respect to the mean flow. The fluid-structure coupling provides a step input to the system, initiating the migration from the rigid solution to the coupled static aeroelastic solution. In general, the static aeroelastic analysis is performed using larger time steps and fewer subiterations than have been shown to be required for a time-accurate temporally-converged solution. This issue is briefly explored later in this paper.

2. Dynamic Aeroelastic Analysis

Dynamic (flutter) analysis is performed in a multistep process, with the dynamic solution started from the static aeroelastic solution at corresponding Mach number, angle of attack and dynamic pressure, and setting the structural damping value to zero. An excitation is provided to the system by adding an initial condition to the generalized (modal) velocities. For all results presented in the current paper, identical values of initial generalized velocity are applied simultaneously to both the plunge and pitch modes. The effects of the initial excitation value on the flutter solution are discussed later in this paper.

The wing response, in the form of the time varying pitch angle, is computed and a logarithmic decrement method is used to calculate the damping ratio. For a stable solution, the damping ratio is greater than zero, and for an unstable solution, the damping ratio is less than zero. To determine the flutter onset dynamic pressure, linear interpolation is performed to find the zero damping case using the two cases on either side of the stability boundary (that is, using the two dynamic pressures where the sign of the damping changes in between them). The flutter frequency is then calculated using the same interpolation coefficients.

Each simulation performed has a different number of time steps and each case has different transient behavior. These two factors mean that the uncertainty associated with each calculated damping value will be different. In the current paper, the uncertainty is captured by standard error values, which are presented along with the damping values in some cases. The standard error of the estimate of the damping value is computed based on the logarithmic decrement process information. The logarithmic decrement technique, as applied, performs a linear fit to the logarithm of the extreme values of the oscillations (that is, the peaks and valleys of the cycles). The damping is computed as in equation 1, where m is the slope of the linear estimate and ω is the estimate of the frequency in radians.

$$\zeta = -\frac{m}{\omega} \quad (1)$$

The standard error estimate of the slope from a linear regression model is calculated as in equation 2, where x_i are the values of the independent variable (time), and y_i are the corresponding values of the dependent variable (the logarithm of the extreme values of the pitch angle). \hat{y}_i are the estimated values of the dependent variable computed using the linear regression model (that is, using the slope and intercept computed from the original data pairs (x_i, y_i)). N is the number of degrees of freedom (the number of peaks and valleys used in the logarithmic decrement process). Note that the number of degrees of freedom is reduced by 2, since 2 parameters (slope and intercept) were estimated to formulate the sample estimates, \hat{y}_i .

$$SE_m = \frac{\sqrt{\frac{\sum_{i=1}^N (y_i - \hat{y}_i)^2}{N-2}}}{\sqrt{(x_i - \bar{x})^2}} \quad (2)$$

The standard error estimate of the damping value is then computed from the standard error estimate of the slope, assigning no error in the calculation of the frequency, equation 3.

$$SE_\zeta = SE_m / \omega \quad (3)$$

IV. Simulation Results

Rigid, static aeroelastic and dynamic aeroelastic analyses were conducted at Mach 0.74 to investigate the influence of separation onset. The angle of attack was varied from -1° to 8° and different excitation levels were applied to the system. Multiple dynamic pressures, each analyzed through an independent simulation, were analyzed at combinations of angle of attack and excitation level.

A. Rigid Steady Simulations

Results from rigid simulations are presented in this section. These results will show that the flow field characteristics change when the airfoil exceeds 6° . This change is shown through surface and volumetric plots (Figure 5), integrated lift coefficients (Figure 6), and pressure field slices (Figures 7 and 8).

In the rigid steady simulations, as the angle of attack increases, the region of flow separation increases and the shock structure moves forward as shown in Figure 5. The rigid steady simulations produce converged results for the simulations below the critical angle of attack of 6° ; above this angle, the solution meanders rather than converges. This meandering behavior is illustrated in Figure 6, which shows the development of the lift coefficient for different angles of attack as the iterations proceed. In Figure 6, the iteration histories corresponding to the highest two angles of attack ($\alpha_0 = 6.5^\circ$ and 8°) do not converge to fixed values. This nonconvergent behavior corresponds to conditions where the flow field is extensively separated and which are outside the range where we think that URANS analysis produces credible results. As previously noted, experimental information does not exist for these higher angles of attack, so this latter assessment is admittedly made without being able to benchmark the computational results.

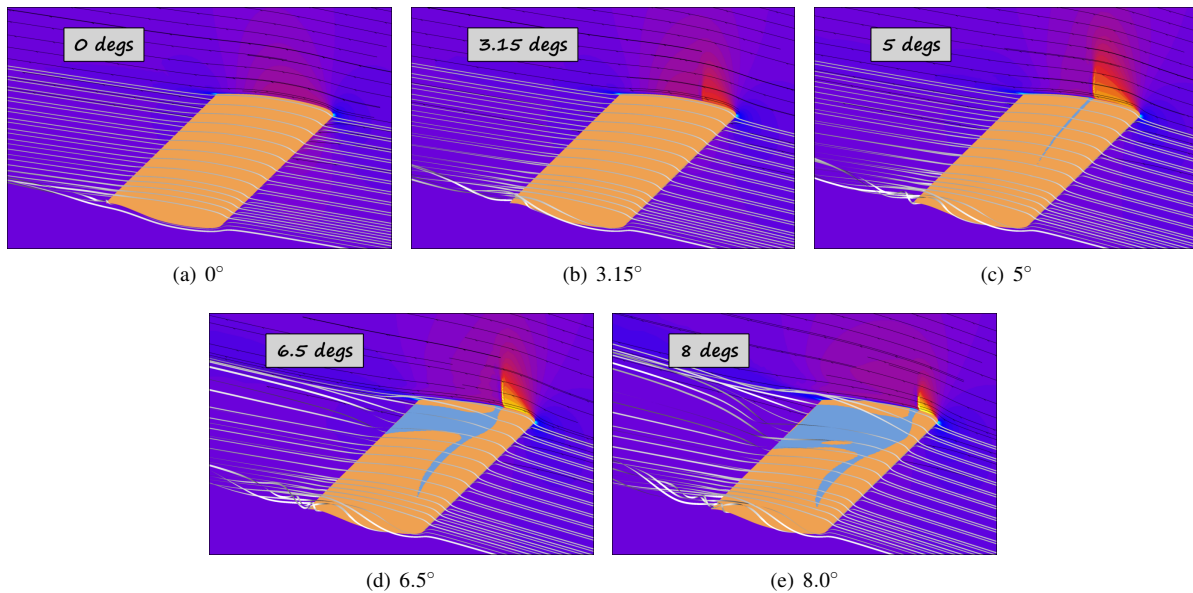


Figure 5. Skin friction surface plots from rigid analysis and Mach contour plots at splitter plate; Snapshots at end of simulation.

Figure 7 shows the pressure coefficient versus nondimensional chord location at the 60% span station on both the upper and lower surfaces for these same angles of attack. In these plots, and all pressure coefficient plots presented, the vertical axis is inverted. As shown in the figure, the shock moves aft with increasing angle of attack for angles below 6.5° and then reverses direction as the angle of attack is further increased. The upper surface shock forms between 1.15° and 2.4° ; the shock continues to gain strength and move aft until 6° . For higher angles, the shock then moves forward with increasing angle of attack, still strengthening.

Aft of the shock, a small region of separation is indicated for angles of attack of 5° and higher, as illustrated in the skin friction plots in Figure 5. In these plots, skin friction is shown on the surface of the wing, with orange indicating positive skin friction (attached flow) and blue indicating negative skin friction (separated flow). On the upper surface, the plots for 3.15° and below indicate no separated flow region. For higher angles, the blue regions indicate the extent of the separated flow region. In these pictures, a slice through the flow field is also shown at the intersection between the splitter plate and the wing root. The contours on this slice show the local Mach number, emphasizing the upper

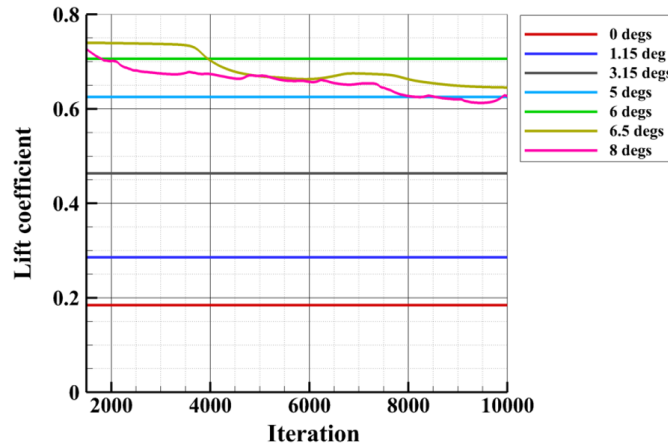


Figure 6. Rigid simulation as iterations proceed; Medium grid.

surface shock location through an abrupt color change, generally from red to purple. The shock extends across the wing, with a small region of separation behind the shock for cases of 5° and above. As the angle of attack increases, the figures show that near the splitter plate, the shock progresses toward the leading edge and is strengthened, indicated by the progression of the color shown in the shock from red to orange to yellow. Near the splitter plate, there is no observed reversal of the direction of shock travel, but the shock appears to weaken near the splitter plate for cases above 6.5° . This is in contrast to the pressure data shown in Figure 7 at the 60% span station. In addition, the separated flow region shown near the splitter plate in Figure 5 is very small in extent in all directions. Starting at 6° , however, there is a larger region of separated flow, shown by the growth of the blue region on the wing as the angle of attack increases.

The plots in Figure 5 also indicate the effect of the tip vortex. The grey streamers in the flow are streaklines, as are the black lines on the slice at the splitter plate. Study of the streaklines shows that the flow over the aft portion of the wing upper surface flows inboard, as well as streamwise. On the lower surface, the streaklines show that the flow moves outboard as well as streamwise. Although the influence of the tip vortex has not been examined in detail in the current work, limited studies were conducted at $\alpha = 5^\circ$ on a two-dimensional airfoil section. This work is incomplete at this point in time and the preliminary results are not presented here, but it was evident that the two-dimensional results were qualitatively different from the three-dimensional results.

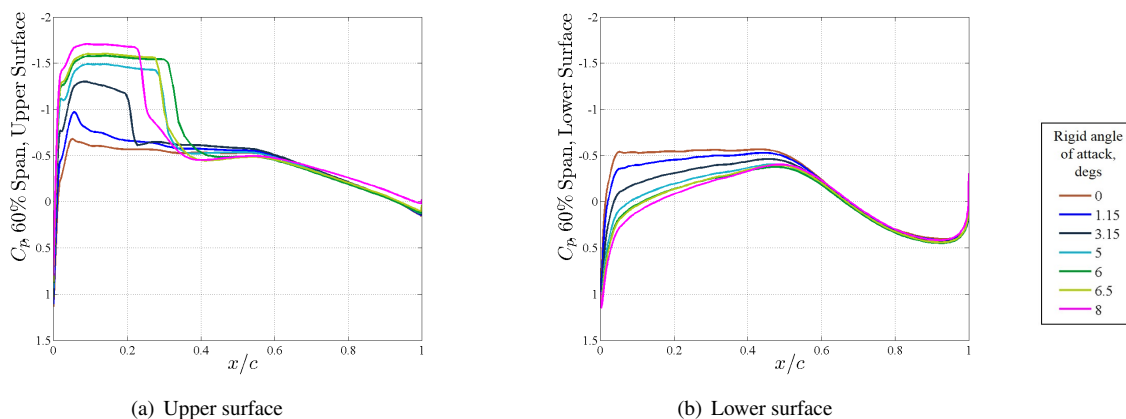


Figure 7. Final time point snapshots of pressure coefficients at 60% span station; Medium grid; Rigid steady analysis.

Comparison of the computational results with experimental results is shown in Figure 8 for selected angles of attack where experimental quantitative information is available. The computational results were taken as snapshots at the last time point from each simulation and are shown by the lines; experimental information is represented by the symbols. The grey shaded regions show the range of the experimental pressure data at the flutter point. The

computations predict the upper surface shock to be stronger and further aft than indicated by the experimental data. This trend is consistent with the trends observed in the AePW data sets.^{4,11} Although the previous work has identified the lower surface aft region as being mispredicted, this trend isn't so much in evidence in the current calculations.

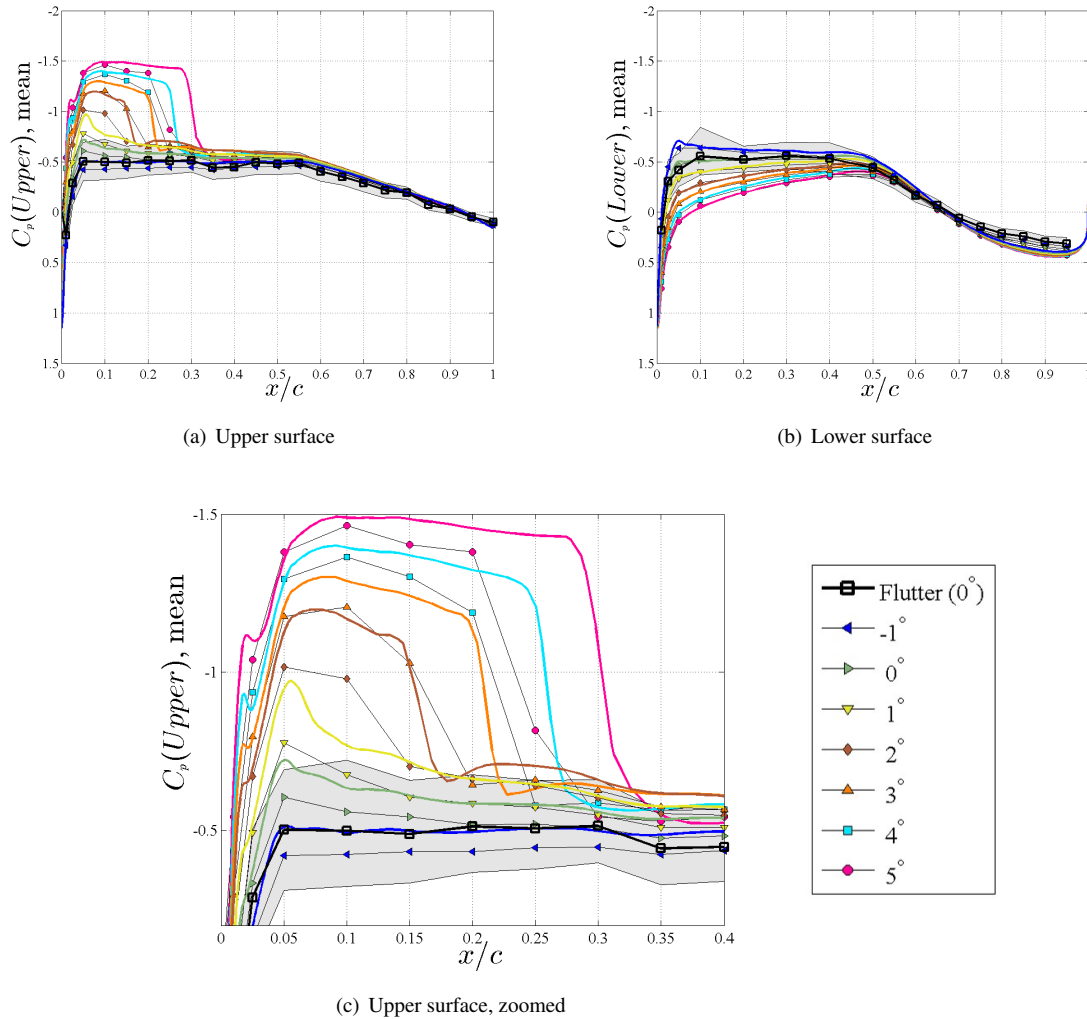


Figure 8. Pressure coefficients at 60% span station; Rigid steady case. Symbols: Experiment. Colored Lines: Analysis. The grey region shows the range for the flutter information from the experiment; Symbols show the mean.

The lift and pitching moment coefficients are shown as functions of angle of attack in Figure 9 for the medium grid. Both the lift and the pitching moment coefficient show linear dependence on the angle of attack until 6° , where dramatic changes in both curves are seen and stall is indicated.

The BSCW airfoil is a supercritical airfoil (SC(2)-0414), so it was designed with the goal of being shock-free at a given lift coefficient; the design lift coefficient for this airfoil is 0.4. Note that at the Mach number of interest for this study, 0.74, a lift coefficient of 0.4 is produced by an angle of attack near 2° . The pressure coefficient plots in Figure 7 show that the shock forms between 1.15° and 2.4° , correlating well with the designed behavior of the airfoil. The coefficient values presented are the final time point of each simulation, not the mean value nor the range of the coefficients. Statistical values should be obtained from time-accurate simulations to better capture the behavior that the method is predicting.

The aerodynamic center and the center of pressure were computed from the coefficient data. The center of pressure is shown in Figure 9c, measured positive aft with the origin at the wing leading edge. The wing chord, 16 inches, was used as the reference length. Thus, the trailing edge location is at a value of 1 in the figure. The center of pressure was calculated from the rigid data, using equation 4 after applying the parallel axis theorem to reference the pitching moment coefficient to the wing leading edge. (The pitching moment coefficient is defined as positive leading edge

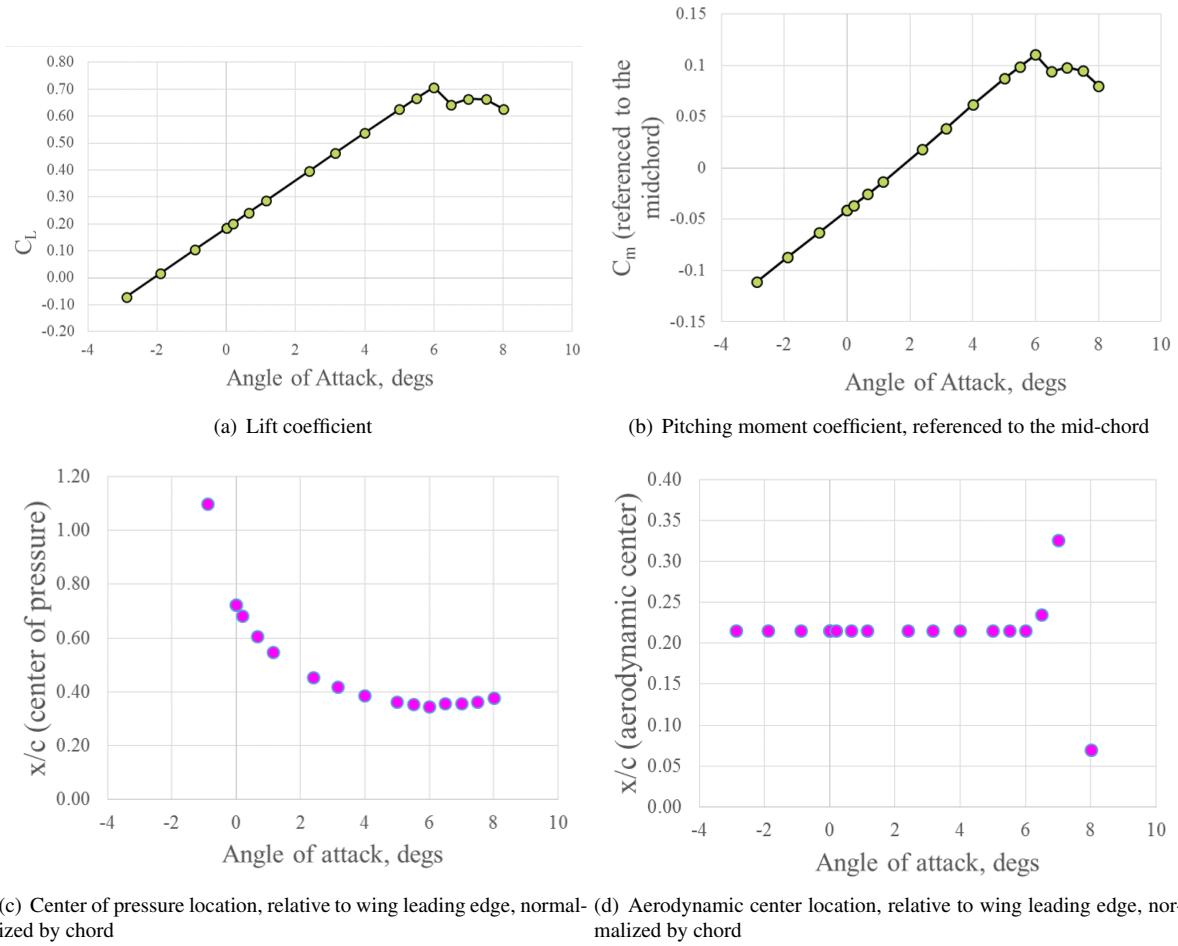


Figure 9. Steady rigid simulation results; Medium grid.

up. The lift coefficient is defined as positive upward. The center of pressure location as defined in equation 4 is thus positive aft from the leading edge.)

$$\bar{x}_{cp} = -\frac{C_m}{C_L} \quad (4)$$

The center of pressure is aft of the trailing edge of the airfoil for negative angles of attack, as shown in Figure 9c. At 0° angle of attack, the center of pressure is aft of the midchord and moves forward as the angle of attack increases. The forward-most position of the center of pressure occurs at 6° and is at 34.6% chord behind the leading edge. Further increases in angle of attack result in moderate migration of the center of pressure aftward. The center of pressure migration is similar to the movement measured and reported in the earliest of airfoil tables for asymmetric airfoils, particularly paralleling those with lower surface cusp regions in the aft portion of the airfoil.²⁴

The aerodynamic center was also calculated from the rigid steady data sets using equation 5.

$$\bar{x}_{ac} = -\frac{C_{m\alpha}}{C_{L\alpha}} \quad (5)$$

The results are shown in Figure 9d. The pitching moment coefficients were calculated relative to the leading edge, thus the location values given are also with respect to the leading edge. In the range where C_L and C_m are linear functions of the angle of attack, the aerodynamic center location is constant (21.5% chord aft of the leading edge). In the region where the behaviors of the coefficients are nonlinear, the aerodynamic center location shifts erratically. Calculations at a refined set of angles of attack in the nonlinear response range would be required to better characterize this movement. The aft shift in the aerodynamic center is produced by separating flow, which will be shown in a later section of this paper to have a destabilizing effect on the system.

B. Static Aeroelastic Results

Static aeroelastic results were generated using the CFD analysis process outlined previously. The static aeroelastic solutions did not develop monotonically and in some cases looked converged for a large number of iterations before migrating to a final equilibrium position. While most of these static aeroelastic solutions were performed with a time step and subiterations that were insufficient to characterize each time step as time-accurate (i.e., the time step was too large and the subiterations too few to declare that the time history points had physical significance), a refined time step solution for $\alpha = 5^\circ$, $\bar{q} = 152$ psf will be examined later in this section.

Static aeroelastic solutions achieve different equilibrium angles of attack based on the rigid (wind-off) angle of attack, the dynamic pressure, the Mach number and the Reynolds number. The latter two parameters are fixed values for this study. Increasing dynamic pressure induces additional twist as it amplifies the influence of the pressure relative to the structural stiffness. This effect is captured in Figure 10, which shows the medium grid predicted aeroelastic twist increment as a function of dynamic pressure for rigid angles of attack from 0° to 5° . The figure shows results from the CFD simulations using circular symbols; square symbols show results from simplified analyses that will be discussed later in this section. In static aeroelastic solutions for rigid angles of attack less than or equal to 1.15° , dynamic pressure induces negative (nose down) aeroelastic twist, reducing the angle of attack. For angles of attack greater than 1.15° , the induced aeroelastic twist angle is positive (nose up) and is linear with dynamic pressure until the total angle of attack exceeds 6.5° . Beyond this condition, additional increase in either dynamic pressure or angle of attack results in increasing the separation region and the shock structure moving forward, producing a corresponding decrease in the total angle of attack. The data sets presented in Figure 10 for $\alpha_0 = 4^\circ$ (green line) and $\alpha_0 = 5^\circ$ (grey line) exemplify the influence of separated flow onset, as nonlinear behavior is observed beginning near 200 psf for $\alpha_0 = 4^\circ$ and 120 psf for $\alpha_0 = 5^\circ$. This will be examined subsequently for the $\alpha_0 = 5^\circ$ case. Note that the change in induced twist direction occurs at the same angle of attack where the upper surface shock forms. That is, for shock-free cases, the induced twist angle is leading edge down; for cases after the upper surface shock has developed, the induced twist angle is leading edge up.

The influence of the separating flow is best observed for the $\alpha_0 = 5^\circ$ case, which is shown in Figure 10 and highlighted in Figure 11. In time history plots of the developing static aeroelastic solutions, there are temporary plateaus in the aeroelastic twist angles before the solution transitions to another equilibrium angle. These temporary plateau values are shown in Figure 11 by the black-filled circles. The grey-filled circles show the final values obtained via the medium grid. The difference in the early versus final solutions is pronounced for dynamic pressures greater than 100 psf, where the computed twist angle deviates considerably, creating a new slope of the line. The quantitative information shown in this figure also includes simulations using the extra fine grid. The extra fine grid results match the early equilibrium (plateau) values from the medium grid solution. It is currently unclear whether the extra fine grid results require additional simulation time and will eventually achieve the reduced angle equilibrium condition or whether the medium grid results produce misleading trends at the higher dynamic pressures. Although extra fine grid results were generated with and without a flux limiter, no significant differences were observed in the static aeroelastic solutions.

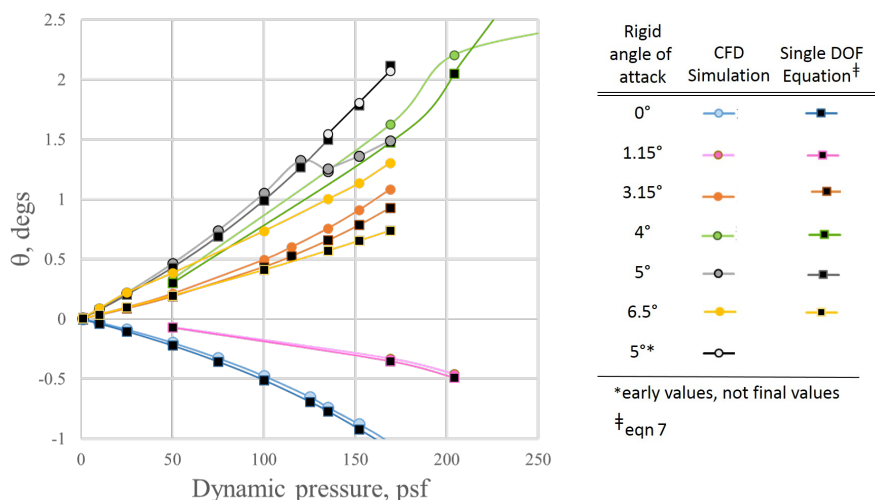


Figure 10. Static aeroelastic twist angles; Medium grid; CFD compared to quasi-steady equation.

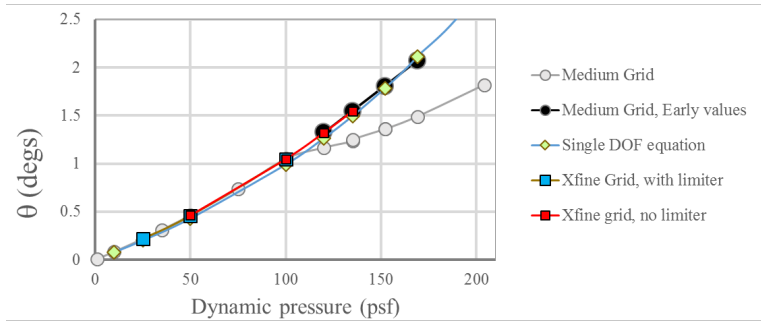


Figure 11. Static aeroelastic twist angles, 5°.

To better understand the transition behavior observed, several simulations with refined temporal parameters were performed. Figure 12 shows results for analyses performed at $\alpha_0 = 5^\circ$, 152 psf. The result labeled “Coarse Temporal Parameters” corresponds to the nondimensional time step size (DT) = 50, dimensional time step size (dt) = 0.0082 seconds, with ten subiterations and Courant-Freidrichs-Lewy (CFL) numbers for mean flow equations = 25 and CFL numbers for turbulence model equations = 50. These parameters were determined by performing a convergence efficiency study at the AePW-2 Case 2 condition (Mach 0.74, $\alpha_0 = 0^\circ$) and correspond to the parameters standardly used for static aeroelastic analyses in the current paper. The result labeled “Fine Temporal Parameters” corresponds to a simulation performed with the parameters used in the dynamic simulations (DT = 1.12, dt = 0.0002 seconds, 200 subiterations maximum, temporal error convergence of 0.10). The two additional simulation results shown are for intermediate choice of time step size and reduced CFL numbers.

In all four cases, the simulations find an initial static twist angle but then migrate to a smaller angle. While the smaller twist angle resembles a stabilized position for a considerable number of iterations in most cases, the continued simulations all show at least one oscillation back toward the original preferred position. For example, the coarse parameter iterations have a hump between 5000 and 5500 iterations where the twist angle changes from 1.4° to 1.5° and then back again. This suggests that one shock location is slightly more stable than the other. The more stable shock location is the forward location, with the wing at a lower angle of attack. The fine time step result shows decaying sinusoidal oscillations with a peak-to-peak range of approximately 0.1° and a down-trending mean value. It is unclear whether or not the mean value will eventually reach the equilibrium position indicated by the larger time step values. Examination of the flow field details makes it clear that the higher angle static aeroelastic simulations correspond to forward shock locations and larger separated flow regions, however, it is unclear what aspect of the solution triggers the transition from one flow state or shock location to the other.

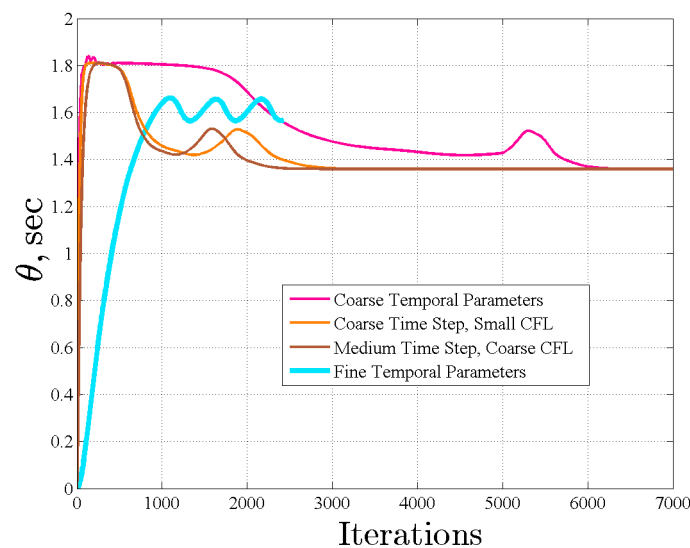


Figure 12. Static aeroelastic twist angles, $\alpha_0 = 5^\circ$, 152 psf; Medium grid; Varying temporal solution parameters.

The dynamic pressure influence on the shock position is illustrated for the case of the medium grid analyses at $\alpha_0 = 5^\circ$ in Figure 13. As the increasing dynamic pressure initially twists the airfoil, the shock moves aft. However, once the airfoil twists such that the total angle of attack is greater than approximately 6.5° , the shock moves forward. This twist exceedance and forward motion is shown in Figure 13 to correspond to cases where the dynamic pressure is greater than 100 psf, which matches the condition where the transitory equilibrium behavior begins.

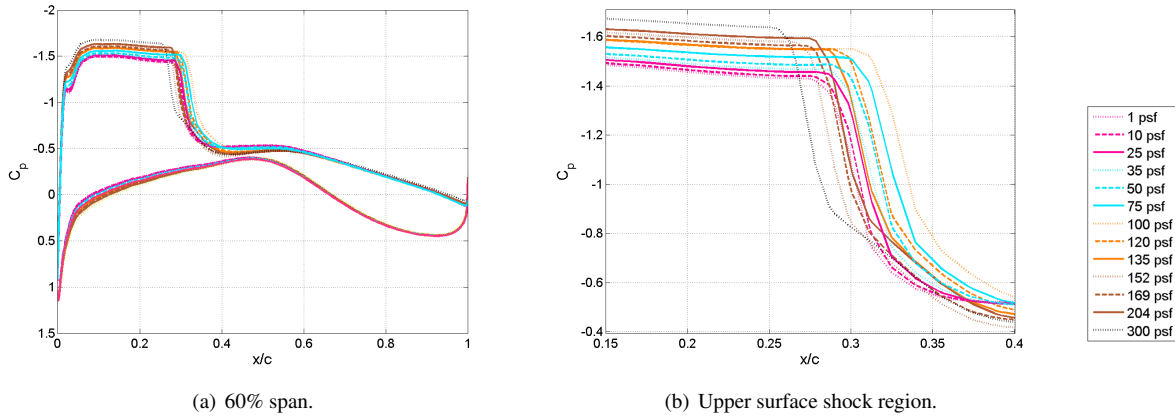


Figure 13. Pressure coefficient distributions from static aeroelastic simulations for various dynamic pressure, $\alpha_0 = 5^\circ$.

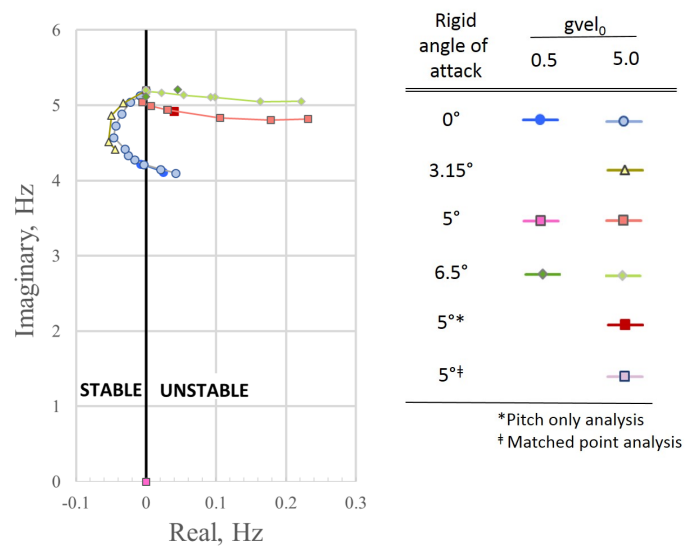
Single degree of freedom estimates of the static aeroelastic twist were also generated based on the rigid static computations. These estimates are useful for trying to understand which cases require analysis using the coupled simulation capabilities and which can be derived from the much-simplified steady rigid procedure. In the case of an aeroelastic system, the total angle of attack is not the rigid angle of attack, but rather is the rigid (wind-off) angle of attack plus the aeroelastically induced twist angle, equation 6. The loads are found by using the linear fit estimates of the aerodynamic derivatives. The flexible static response using the linear method is calculated by setting the aerodynamic moment equal to the structural restorative moment. This results in an expression for the aeroelastic twist angle given in equation 7, where $\bar{\alpha}$ is the rigid angle of attack plus a bias angle found as the x-intercept of the plot of pitching moment coefficient versus angle of attack. The comparison results are shown in Figures 10 and 11. Examining the results, it is only post-stall that the coupled CFD static aeroelastic characteristics deviate significantly from those derived from the single degree of freedom rigid simulations.

$$\alpha_{total} = \alpha_0 + \theta \quad (6)$$

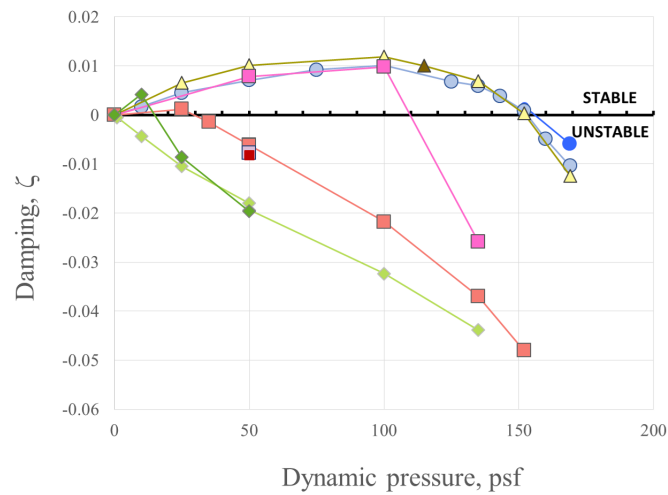
$$\theta = \bar{\alpha} \frac{1}{\frac{K_\theta}{\bar{q} - S * c * C_{m\alpha} - 1}} \quad (7)$$

C. Dynamic Aeroelastic Simulations

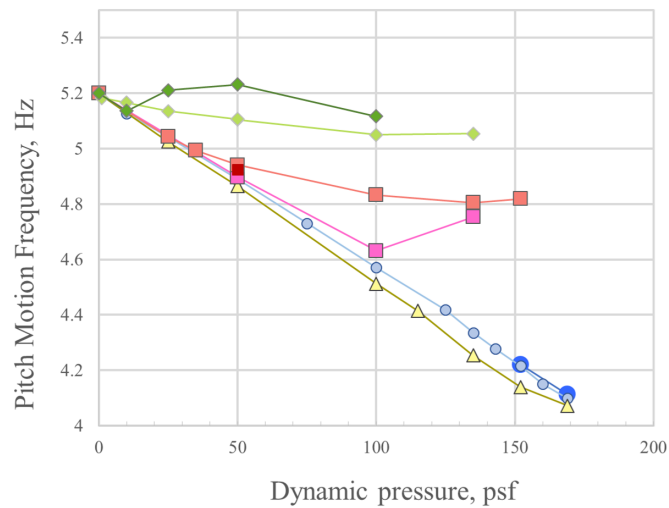
Dynamic aeroelastic simulation results are produced by applying an initial perturbation of generalized velocity to the coupled system equations, as described in Section B. The coupled system is observed to respond in an oscillatory manner, and the time histories are analyzed. For the BSCW at Mach 0.74, there are different flow field scenarios in the dynamic simulations: attached flow, separated flow and separating/attaching flow. Summary plots of the medium grid flutter results are shown in Figure 14 for four angles of attack (0° , 3.15° , 5° and 6.5°) and two values of generalized velocity excitation ($gvel_0 = 0.5$ and 5). The root locus plot, Figure 14a, shows the progression of the pitch eigenvalue as dynamic pressure increases. Figures 14b and c show damping and frequency values, respectively, versus dynamic pressure for the medium grid simulations. Time histories of the aeroelastic pitch angle increment, θ , for flutter onset conditions are shown in Figure 15 for rigid angles of attack of 0° , 3.15° and 5° . Time histories of pitching moment coefficient and θ for the same angles and also 6.5° are shown in Figure 16. The pitching moment coefficient time histories (blue lines) emphasize the change in the physics that occurs for the $\alpha_0 = 6.5^\circ$ case, shown by the nonlinear responses. The aeroelastic pitch angle increments vary sinusoidally and smoothly throughout, as shown by the green lines in Figure 16.



(a) Root Locus.



(b) Damping vs. Dynamic pressure.



(c) Frequency vs. Dynamic pressure.

Figure 14. Flutter results; Medium grid

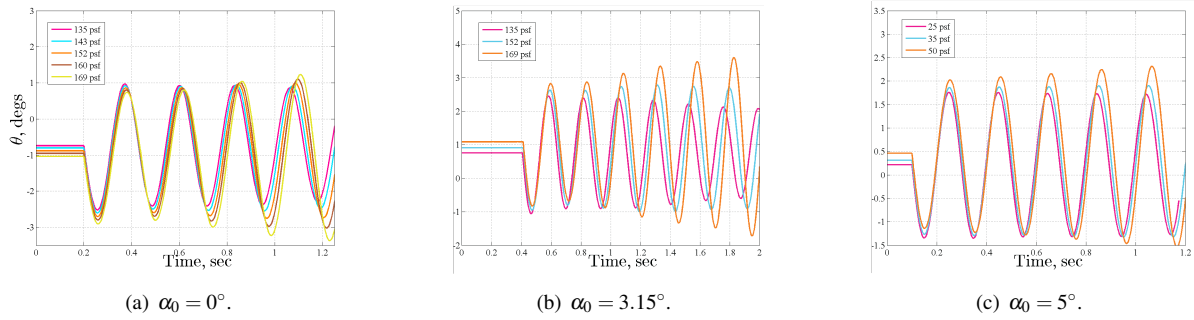


Figure 15. Time histories of analyzed conditions above and below the flutter conditions; Medium grid.

For the 0° angle of attack case, the flow is attached without an upper surface shock. Here, the static aeroelastic solution (see Figure 10) induces approximately 1° nose down twist, reducing the total effective angle of attack. All of the time histories (see Figures 15a and 16a) appear perfectly sinusoidal. The resulting flutter onset as seen in Figure 14 occurs at a dynamic pressure of 152 psf, which is 10% below the experimentally measured onset dynamic pressures of 169 psf. The pitch mode frequency is seen to migrate smoothly and monotonically from the rigid pitch mode frequency at 5.2 Hz, down to 4.2 Hz at flutter onset. The damping trend is similarly smooth, with the maximum damping calculated at 100 psf. The flutter onset results are nearly identical for both values of perturbation velocity, $gvel_0$, shown in Figure 14.

The behavior of the pressure field for different parts of the oscillation cycle is shown in Figure 17. For this case, there is no upper surface shock and no separated flow, but a shock does appear on the lower surface at the extreme negative angles of attack. Information is presented at three dynamic pressures in Figure 17: below flutter onset (subplot a, $\bar{q} = 135$ psf); the closest case to flutter onset (subplot b, $\bar{q} = 152$ psf) and post-flutter (subplot c, $\bar{q} = 169$ psf). In each subplot, there are four graphics. The top graphic shows the time history of the aeroelastic twist angle increment, θ , with six specific time points identified at the oscillation peaks and valleys. The second graphic shows the snapshots of the pressure coefficient distribution at 60% span as a function of chord. Snapshots of the upper surface pressure distribution are only shown at the time points identified in the top figure with colored symbols. The line colors in the second graphic correspond to the symbol colors in the first graphic. Snapshots of the lower surface pressure distribution are shown for all time points with the same color-coordination as the upper surface snapshots. Snapshots corresponding to time points that aren't specially identified by symbols in the top graphic are colored brown.

The dominant feature of the snapshots is the brown region that shows the range of the lower surface pressures. Each valley identified in the oscillation, corresponding to the lowest aeroelastic twist angle and thus the lowest angle of attack, corresponds to a lower surface shock at the aftmost position on the chord. The shock position repeats nearly identically for the three identified valley points. The third graphic in each subfigure shows a zoomed region of the time history of the aeroelastic twist angle, focused on the time range with the points previously identified. These identified time points are aligned with the time axis in the fourth graphic. The fourth graphic is a contour plot of the pressure coefficient on the upper surface, shown as a function of chord (vertical axis) and time (horizontal axis). For the 0° case, the upper surface behavior is very benign, and the contour plots show little.

Attached flow with an upper surface shock is seen in the case of $\alpha_0 = 3.15^\circ$. Here, the static aeroelastic solution shows an increased angle of attack as dynamic pressure increases in Figure 10. Static aeroelastic solutions were only performed at dynamic pressures up to 169 psf. At this maximum condition, the total angle of attack was less than 6.5° . The dynamic solutions, using $gvel_0 = 5.0$ produced a flutter onset condition nearly identical to that produced at 0° , as shown in Figure 14. Time histories of integrated quantities are all nearly perfect sinusoids as seen in Figure 16b. The time histories of pressures, Figure 18, show nonlinear behavior as the shock oscillates forward and aft with the pitch angle.

Figure 18 is similar in format to Figure 17 and the reader is referred to the detailed description of Figure 17 to better understand the layout. The differences for the $\alpha_0 = 3.15^\circ$ case are highlighted here. Snapshots of both the upper and lower surface pressure distributions are shown for the identified time points, color-coordinated with the symbols in the top graphic as discussed for Figure 17. Here, however, the upper surface snapshots are shown for all time points by the citrus colored region.

For the cases at $\alpha_0 = 3.15^\circ$, there is an upper surface shock, but the flow is not separated. Thus, the aftmost shock position occurs when the angle of attack is at the peak value. The movement of the shock is monotonic as the alpha value increases to that peak and monotonically decreasing as the angle of attack decreases away from that peak. This is shown by the snapshots as well as the color contour plot in the bottom graphic for each case. The three subplots

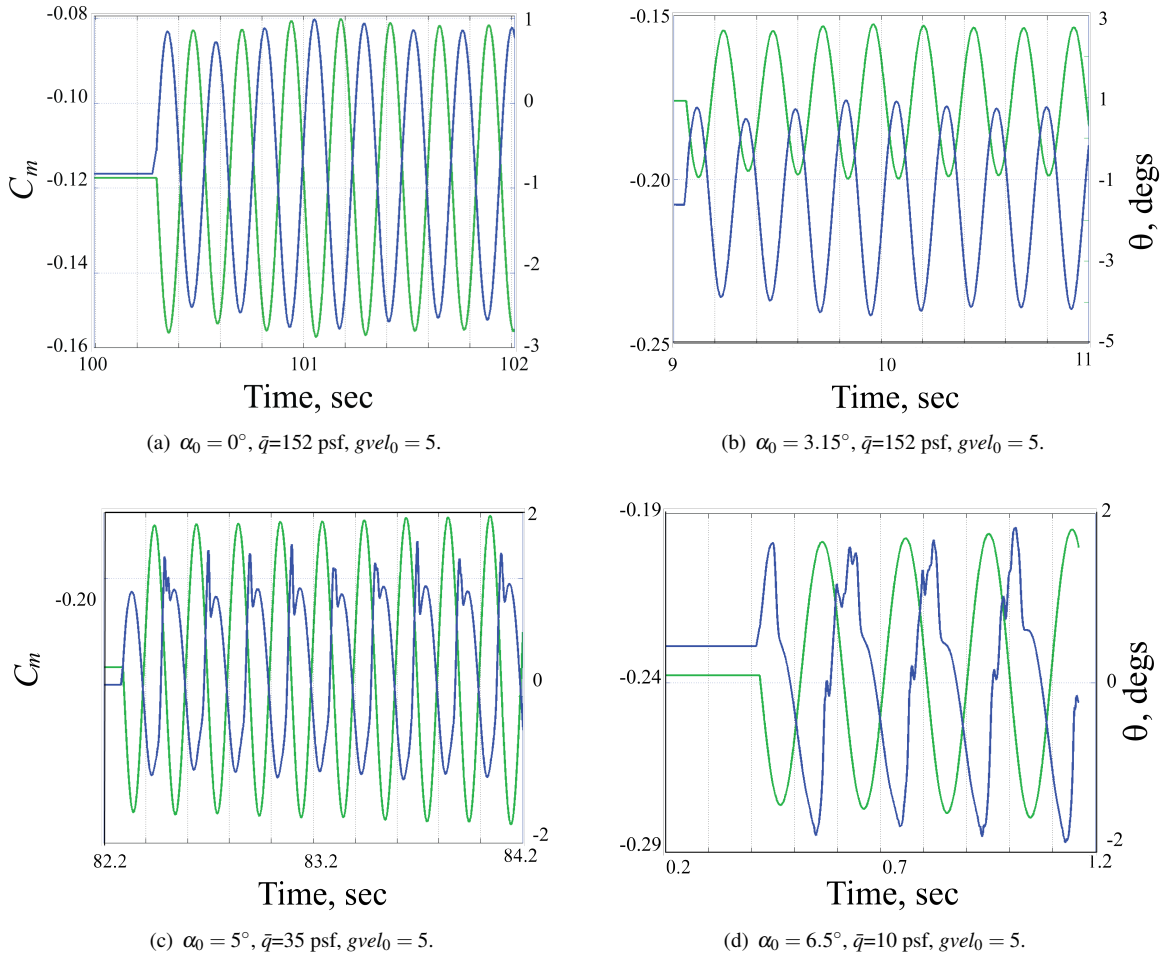


Figure 16. Time histories of analyzed conditions nearest the flutter conditions; Medium grid.

show increasing dynamic pressure, with Figure 18 showing the behavior for an unstable case. The time history shows a growing amplitude oscillation and the snapshots show that the upper surface shock moves further forward with each oscillation through the negative aeroelastic angle range. Here, the total angle of attack is approaching 0° . On the contour plot, the supersonic region ahead of the shock is shown by the dark blue regions which transition abruptly to lighter blue regions as the pressure changes rapidly across the shock. The sinusoidal pattern formed by the edges of the dark and light blue regions shows that the pressures associated with the upper surface shock structure oscillate sinusoidally in time.

The most thorough exploration of the dynamic solution results was done at a rigid angle of attack of 5° . Here, the flutter onset boundary was computed for fixed excitation amplitudes of 0.5 and 5.0. From the results shown in Figure 14, at $gvel_0 = 5$, the system was unstable at $\bar{q} = 35$ psf for the medium grid results and Figure 15c indicates that the initial positive direction oscillation angle of attack reached 6.7° . The phase relationship between the angle of attack and the shock movement shifted by 180° (i.e., there is a sign change). Linear interpolation between results at $\bar{q} = 25$ and $\bar{q} = 35$ psf gave an estimate of flutter onset at $\bar{q} = 30$ psf.

The behavior of the pressure distribution for different parts of the oscillation cycle are presented for $\alpha_0 = 5^\circ$ cases at three dynamic pressures in Figure 19. For the $\alpha_0 = 5^\circ$ cases, flow separation intervenes and the shock movement is not monotonic and the aftmost position of the shock doesn't occur when the angle of attack is largest. The aftmost shock location occurs when the total angle of attack reaches approximately 6.5° . This is observed most readily by examining Figure 19c, which shows the post-flutter behavior. The aftmost shock position is shown in the snapshot pressure distribution plot by the blue line. This snapshot corresponds to a time point near 201.35 seconds, identified by the blue square symbol in the graphics of the aeroelastic twist angle time histories. This time point is also indicated on the contour plot by the black dashed line. The black dashed line passes through the aftmost point on the dark blue

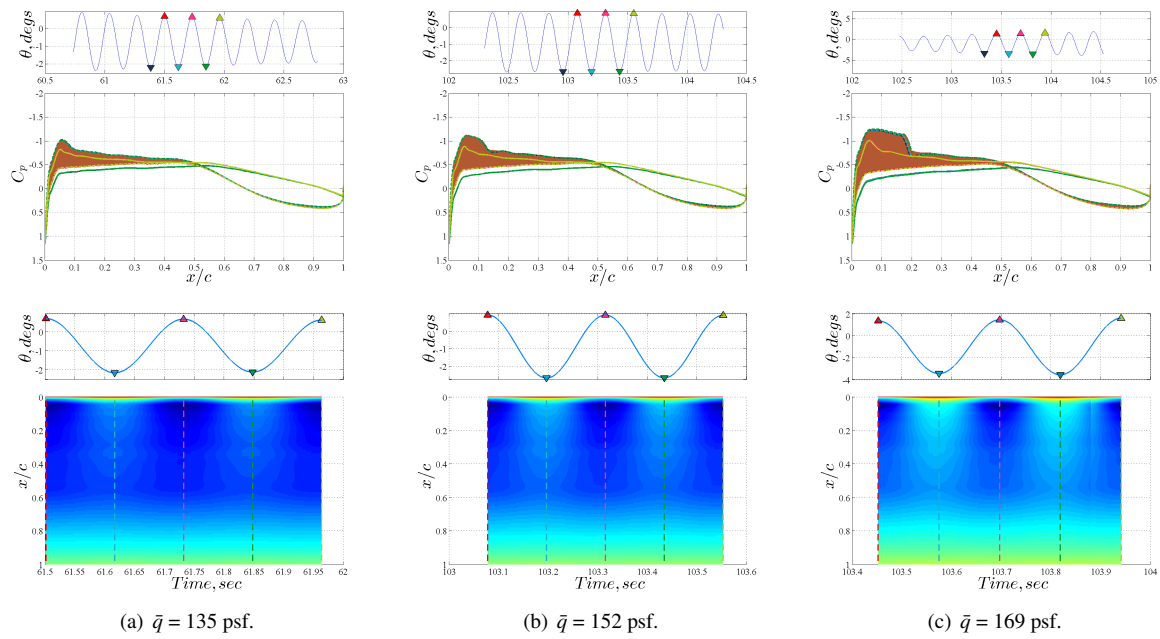


Figure 17. Pressure behavior during oscillations, $\alpha_0 = 0^\circ$.

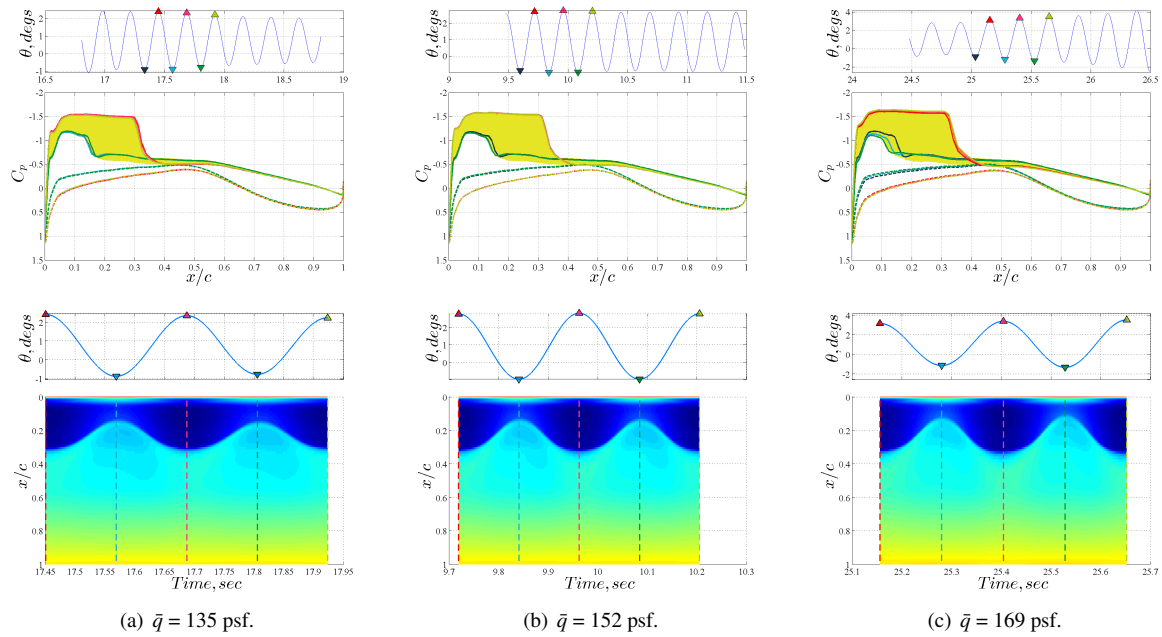


Figure 18. Pressure behavior during oscillations, $\alpha_0 = 3.15^\circ$.

region on the contour plot. As described previously, the dark blue regions correspond to the supersonic plateau ahead of the shock. As the angle of attack continues to increase during the oscillation, the shock movement changes direction and moves forward. The forward movement halts as the pitching oscillation cycle progresses; the direction of shock travel changes when the total angle of attack decreases back to below 6.5° . To better illustrate the movement of the shock with the angle of attack change, a three-dimensional plot for an example case is shown in Figure 20 for $\alpha_0 = 5^\circ$, $\bar{q} = 100$ psf.

Frequency analysis of time histories of the pressures and the pitching moment coefficient show dynamics at the flutter frequency (or the aeroelastic primary coupled frequency) but also at two, three and five times the flutter frequency. Rather than being superharmonics due to data processing, features of the time history data can be traced to each of these frequency multiples as the shock reverses over portions of the oscillation cycle.

The bottom of the transonic dip of the flutter boundary appears to coincide with separating/reattaching flow physics. At Mach 0.74, using the medium grid, this occurs at $\alpha_{total} = 6.5^\circ$, where the flutter simulations without flux limiter and with standard perturbation velocity induce flutter for every dynamic pressure, from 0 psf to 300 psf. This is not to say that the predicted flutter onset at 0 psf is physically meaningful. The nonlinear responses in the pitching moment coefficient indicate that the simulated flow fields are different from the flow fields predicted at the lower angles of attack.

1. Matched Point & Single Degree of Freedom Analyses

The flutter summary plots for the medium grid simulations, shown in Figure 14, include two additional cases that haven't been discussed: matched point analysis and pitch-only analysis simulations at $\alpha_0 = 5^\circ$, $\bar{q} = 50$ psf with an initial generalized velocity perturbation of 5.0. Simulating a matched point condition means having Mach number, dynamic pressure and Reynolds number all corresponding to the same physical condition. This analysis result, shown by the lavender-filled square on each subplot in Figure 14, indicates that there is little influence on the damping or frequency value as it closely matches the result for the nonmatched condition.

The second additional case is shown in Figure 14 by the dark red squares. This simulation was performed using only the pitch degree of freedom in the structural model. The results, again, show little influence on the damping or frequency. This result shows that, for this specific case, the flutter mechanism is a single degree of freedom—pitch-only—instability. It has not yet been evaluated whether this is true for all of the cases, or if possibly this is only true for those cases that are seen to deviate from the upper arch of results shown on the damping plot, Figure 14b. If the latter is true, this would indicate a change in instability mechanism due to amplitude of perturbation, as well as angle of attack.

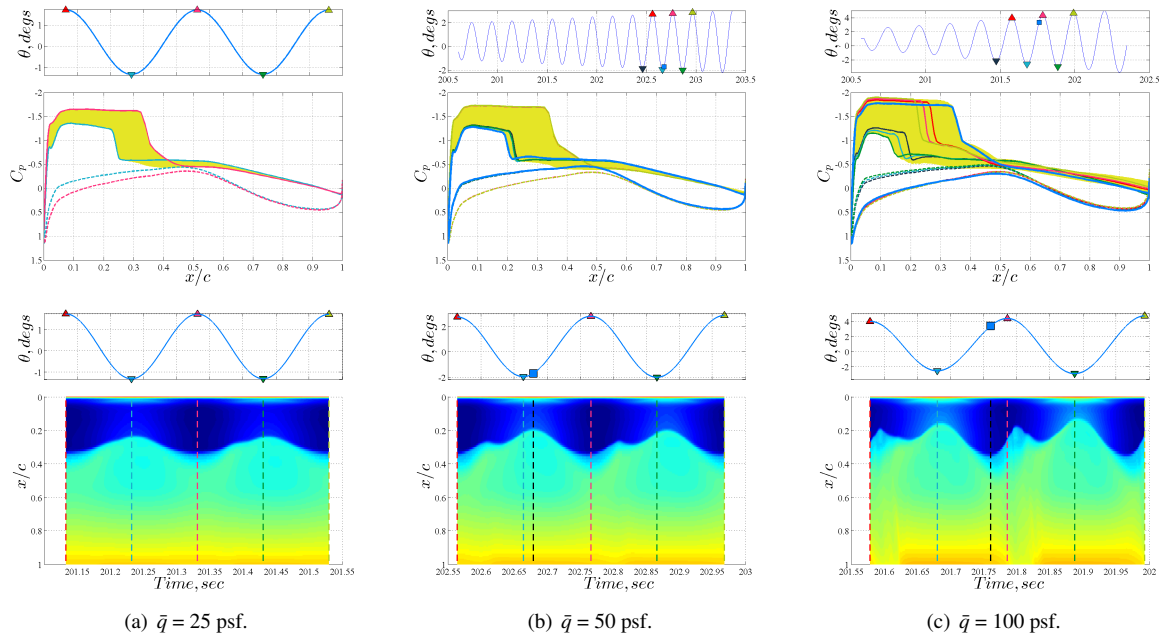


Figure 19. Pressure behavior during oscillations, $\alpha_0 = 5^\circ$.

2. Spatial Resolution Effects

Dynamic aeroelastic analyses were also performed using the extra fine grid. Summary flutter results are shown in Figure 21 for three rigid angles of attack (5° , 6.5° and 8°) and two values of initial generalized velocity (0.5 and 5.0). The system was unstable at $\bar{q} = 75$ psf; linear interpolation using results at $\bar{q} = 50$ and $\bar{q} = 75$ psf gave an estimate of flutter onset at $\bar{q} = 60$ psf. This is substantially higher than the flutter prediction from the medium grid results, $\bar{q} = 30$ psf. The discrepancy between the two grid results is in contrast to the results produced for AePW-2 at Mach 0.74, $\alpha_0 = 0^\circ$, where the grid size had almost no impact on the predicted flutter onset condition. The result does agree well, however, with the trends observed in the AePW-2 results at Mach 0.85, $\alpha_0 = 5^\circ$, where the spatial resolution (grid size) has been shown to have a substantial effect on the flutter prediction.² The requirement for increased spatial resolution

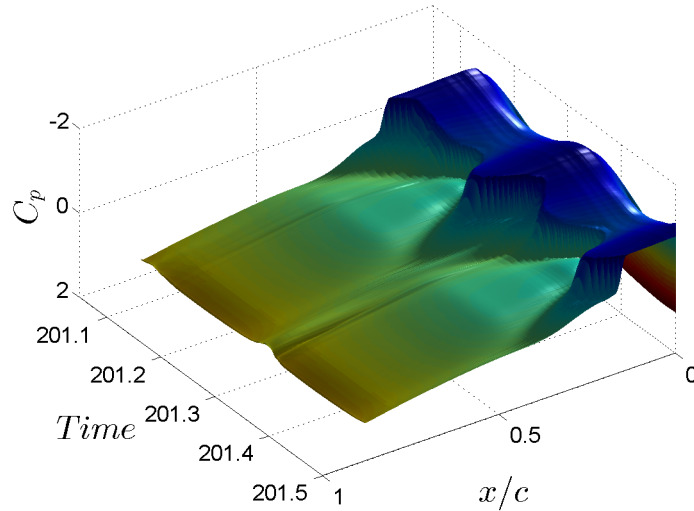


Figure 20. Pressure behavior during oscillations, $\alpha_0 = 5^\circ$, $\bar{q} = 100$ psf.

appears to be driven by the presence of separated flow. Additionally, at $\bar{q} = 50$ psf, where the system analyzed with the extra fine grid was stable, the positive direction oscillation angle reached a maximum of 7.02° . This indicates that the critical angle of attack is slightly higher than the critical angle predicted using the medium grid ($\alpha = 6.5^\circ$). No experimental data set is available to verify either prediction, however.

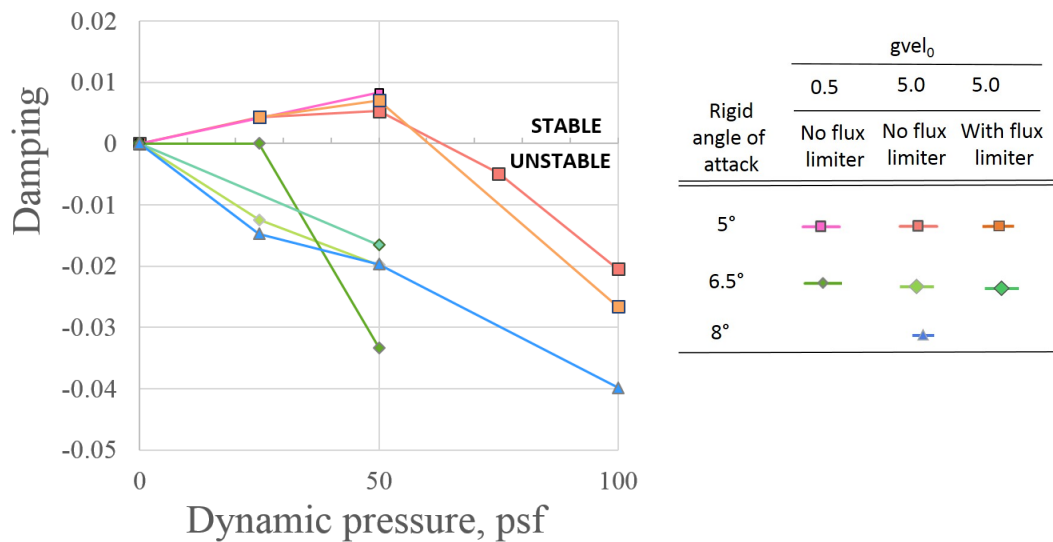


Figure 21. Flutter results; Extra fine grid.

3. Initial Perturbation Effect

The typical flutter calculation in FUN3D begins with an initial excitation “kick” at the start of the dynamic aeroelastic simulation. In the current paper, this kick was applied in the form of an initial value of generalized velocity. The magnitude of the kick is somewhat arbitrary; however, it cannot be so large that it causes large grid deformation and possible solution failure. A large kick in the pitch degree of freedom may also change the aerodynamic state of the flow, leading to incorrect flutter prediction for systems assumed to be subject to small perturbations in freestream conditions. On the other hand, a kick that is too small will result in the solution taking a very long time to develop.

In reference 2, the notion that an initial excitation kick might not be required to obtain a flutter solution was explored. Rather than applying a fixed magnitude perturbation, reference 2 explored the concept that the change in going from the rigid steady solution to the coupled aeroelastic solution would be sufficient to perturb the system and assess flutter. The damping value for the case examined using this modified perturbation method was similar to the value extracted using the nominal perturbation ($gvel_0 = 5$) applied in the current work, implying that the step input associated with applying the aeroelastic coupling is approximately equivalent to a perturbation level of 5.

In the current work, the influence of the initial perturbation level on the flutter onset boundary was assessed at $\alpha_0 = 0^\circ$ and $\alpha_0 = 5^\circ$ angles of attack at fixed dynamic pressures, using the medium grid. The damping values extracted for these cases are presented in Figure 23. At $\alpha_0 = 0^\circ$, dynamic pressures of 152 and 169 psf were examined. The damping values for these cases are shown to be gradual, monotonic and nearly constant slope functions of the initial perturbation level.

The flutter onset boundaries assessed in terms of the perturbation size at 5° angle of attack show more complicated dependence. As shown in Figure 22, time histories resulting from an initial assessment at a dynamic pressure of 100 psf show significantly different characteristics for cases with values of $gvel_0 = 0.5$ and 5. The figure shows the smooth sinusoidal variation of the pitch angle, overplotted with the pitching moment coefficient. For the large perturbation level, the pitching moment coefficient shows nonlinear characteristics, particularly at the peak of the pitching moment coefficient, corresponding to the time points just after the angle has reached the maximum value.

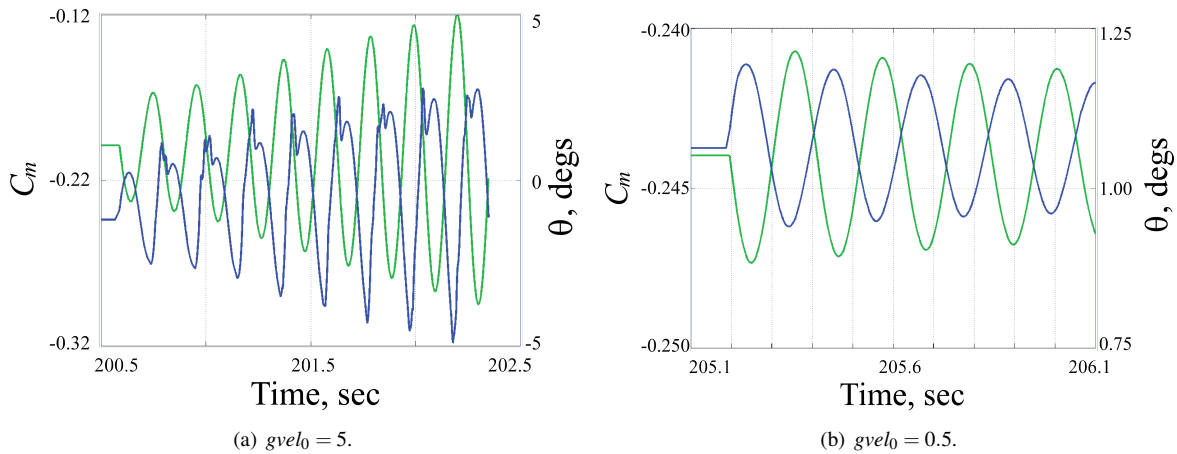


Figure 22. Time histories $\alpha_0 = 5^\circ$, 100 psf; Medium grid.

To further explore the effect, additional levels of perturbation were evaluated. Values of $gvel_0 = 0.5, 1, 1.5, 2, 3$ and 5 were used to excite the simulation; the damping results are presented in Figure 23. For $gvel_0$ greater than or equal to 1.5, the initial positive direction oscillation went to $\alpha = 6.5^\circ$, and the system destabilized. The lower two perturbation level cases (0.5 and 1.0) were stable. The damping values indicate that there is a distinct transition in the physics between the simulations at 1.0 and 1.5. As shown in Figure 10 for the $\alpha_0 = 5^\circ$, $\bar{q}=100$ psf case, the static aeroelastic twist angle is 1.05° . A plot showing the absolute value of the dynamic portion of the aeroelastic twist angle is given in Figure 24. The orange line shows the results for the stable $gvel_0 = 1$ case, which has a first oscillation peak amplitude of 0.3° ; the brown line shows the unstable results for the $gvel_0 = 1.5$ case, which has a first oscillation peak amplitude of 0.5° . Combining the rigid angle of attack (5°), the static aeroelastic twist angle (1.05°) and the dynamic peak angles for the two cases on either side of the stability boundary produces values of $\alpha_{total} = 6.35^\circ$ and 6.55° . Note that the first is stable and the second is unstable, reinforcing the interpretation that cases with a maximum angle of attack less than 6.5° are stable, while cases that exceed this angle are unstable.

4. $\alpha_0 = 6.5^\circ$ Cases

For $\alpha_0 = 6.5^\circ$, out of all the simulations performed, there is only one solution that might be considered as neutrally stable. All the others are unstable. Two example results from the medium grid simulations, both showing erratic progression and instability, are shown in Figure 25. The extra fine grid at $\bar{q} = 25$ psf with a $gvel_0$ of 0.5 shows an oscillation in pitch angle that, while oscillating erratically, doesn't diverge over the cycles performed. Results discussed earlier for the extra fine grid also indicate that the critical angle is in excess of 7° , so this case may not have sufficient excitation to achieve the critical angle. In general all of the simulations at $\alpha_0 = 6.5^\circ$ contained long and

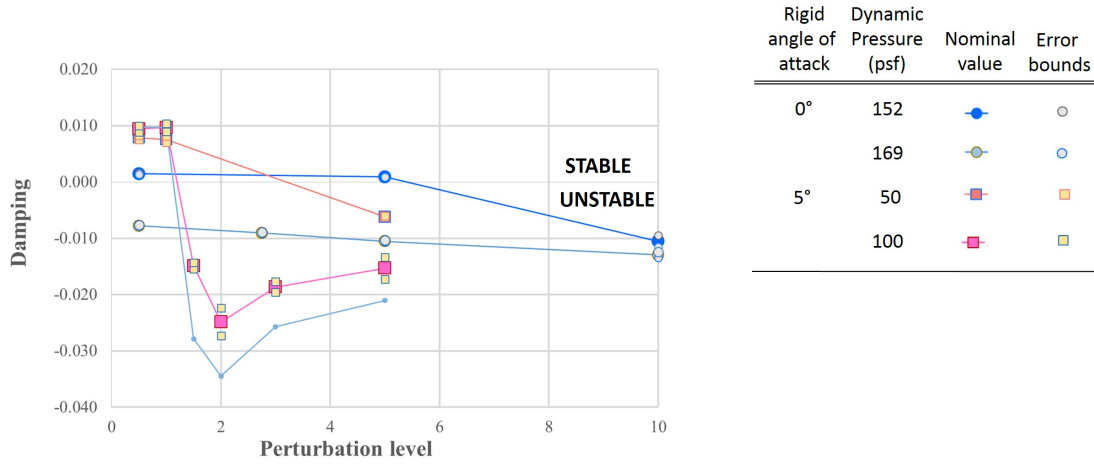


Figure 23. Flutter results; Medium grid; Damping variation with initial perturbation level.

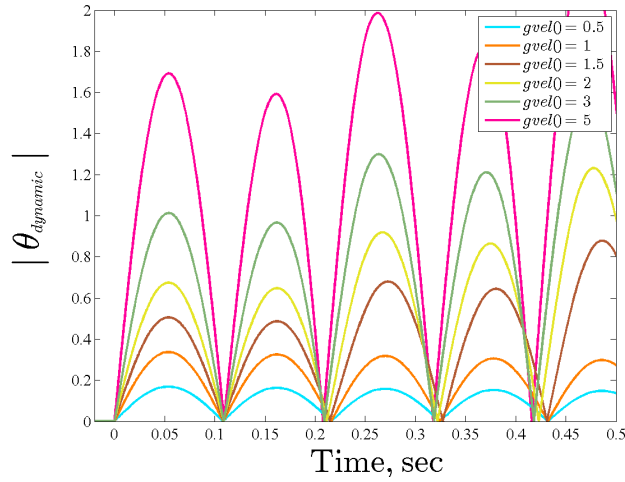


Figure 24. Flutter Results, $\alpha_0 = 5^\circ$, 100 psf; Medium Grid; Variation of the absolute value of the dynamic portion of the aeroelastic twist angle with initial perturbation level.

variable transient regions; many of the solutions also appear to change macroscopically due to computer round-off. These are matters for continued exploration.

V. Continuing Analyses

The companion publication to this work, reference 2, indicates that the back side of the flutter bucket (transonic dip) for the 5° angle of attack condition is near Mach 0.82. The flutter boundary across the transonic Mach range at 5° angle of attack, produced in reference 2, is reproduced here in Figure 26. As the angle of attack increases, the transonic dip of the flutter boundary has historically been observed to shift to the left (i.e., to a lower Mach number), exemplified by Figure 1. Based on the steady rigid results, 8° was investigated as a candidate angle of attack to see if the transonic dip would be shifted to below Mach 0.74. That is, $\alpha_0 = 8^\circ$ was explored to see if the flow was sufficiently separated such that the transonic dip of the flutter boundary would be moved to a lower Mach number. If so, this would produce a higher dynamic pressure for flutter onset, as was observed at Mach 0.82 for $\alpha_0 = 5^\circ$. The extra fine grid was used for this investigation. The results did not show the desired shift to a lower Mach number, with the damping values indicating that the 8° system is not more stable than the 6.5° system for corresponding dynamic pressures. Thus, the back side of the flutter bucket is predicted to be at a Mach number greater than 0.74 for $\alpha_0 = 8^\circ$. Higher angles of attack could be examined, but it seems likely that we have already applied the URANS analysis to conditions beyond the range where they are credible. Without experimental data to benchmark against, further exploration extending the

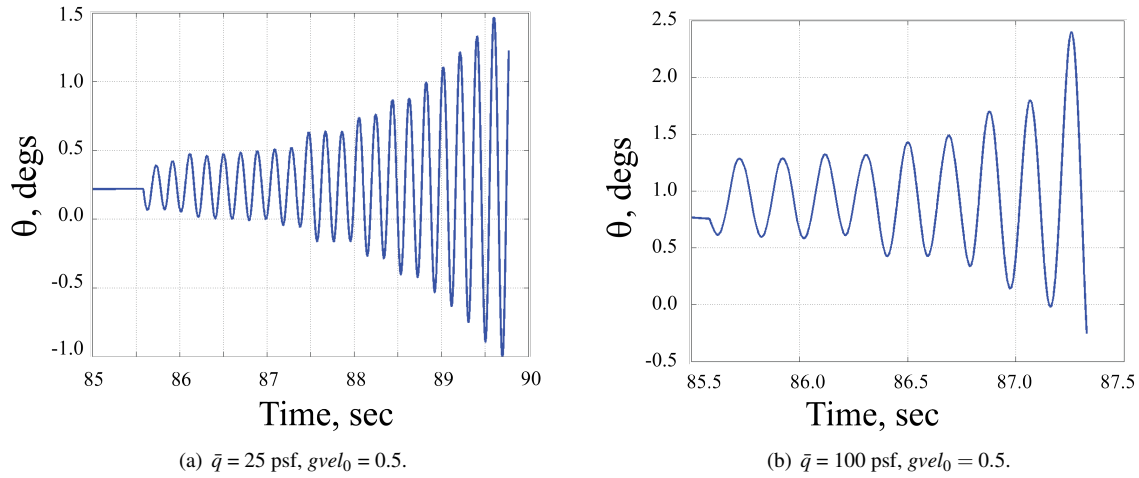


Figure 25. Example time histories, $\alpha_0 = 6.5^\circ$; Medium grid.

angle of attack range above 8° doesn't seem fruitful.

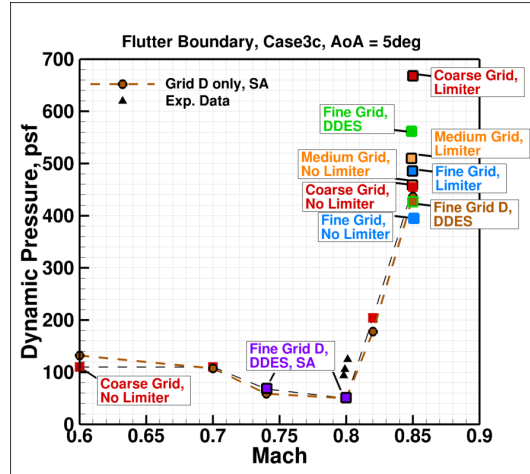


Figure 26. Flutter boundary assessment, Mach 0.6 - 0.85, $\alpha_0 = 5^\circ$ using FUN3D, from reference 2.

The results shown in Figure 26 overlap the results in the current paper at Mach 0.74. Note that in these results, the back side of the transonic dip for $\alpha_0 = 5^\circ$ is predicted to begin by Mach 0.82, as indicated by the increased flutter dynamic pressure. The small triangular symbols in Figure 26 show the experimental points that were produced at nearby angles of attack. The measured angles of attack for these unstable conditions were 5.3° , 5.4° and 5.5° . No mention was made in the publications of the experimental data that a flutter-free pass was made below these conditions. This suggests that the flutter onset condition could be even lower than the instability points reported. These experimental points give some confidence that the flutter predictions in this range are reasonable, although this comparison is far from conclusive.

Flutter computations are currently being performed at higher angles of attack at Mach 0.74 to attempt to identify the edge of the transonic flutter bucket, that is, the point at which the flow remains separated and the flutter onset condition rises. At Mach 0.80, simulations are being performed at angles of attack between 5° and 10° to attempt to establish the onset of the back side of the flutter bucket. Additional studies that may be pursued include modeling the system with a Lattice Boltzman approach, explicit modeling of the splitter plate, more detailed examination of the influence of the tip vortex, matched point condition effects, mapping the flutter envelope explicitly using only the pitch degree of freedom, and revisiting the two-dimensional airfoil configuration to better understand the influences of the wing tip vortex.

VI. Conclusions

The transonic dip of the flutter boundary encountered by the BSCW is due to separating/reattaching flow. Using a medium grid with 9 million nodes, the critical angle for this condition at Mach 0.74 is predicted to be 6.5° . The predicted angle is slightly larger using an extra fine grid with 35 million nodes. Effects of this critical angle are seen in the rigid steady results as a reversal in the shock position with increasing angle of attack. The effects are seen in the static aeroelastic solutions as reductions in the total angle of attack with increasing dynamic pressure when the total angle of attack exceeds 6.5° . The effects seen in the dynamic aeroelastic solutions are a change in the phase of the FRFs of the pitching moment coefficient when the dynamic pressure exceeds the flutter condition. Examination of the shock movement over a cycle showed the same reversal as observed in the steady rigid and static aeroelastic solutions. This behavior leads to different frequencies being significantly represented in the responses. This isn't a superharmonic effect, but rather the effect of separation onset part way through the cycle.

Different perturbation levels used to provide initial excitation at the start of the dynamic analyses give different flutter boundaries when separation onset is part of the flutter inducement (i.e., within the transonic dip region). When separation is not a factor, the perturbation level matters little. At Mach 0.74, the transonic dip of the flutter boundary is defined by solutions perturbed such that they reach 6.5° total angle of attack. At other transonic Mach numbers, it is anticipated that there are similar critical angles. It is also anticipated that the critical angle of attack will be lower at higher Mach numbers and higher at lower Mach numbers. Additional experimental quantitative information is needed to assess where the simulation represents physical reality.

VII. Acknowledgments

The authors thank the NASA Transformational Tools and Technologies project and the NASA Engineering and Safety Center for sponsoring this work. We also thank the FUN3D developers and Robert T. Biedron in particular. Bob's efforts to improve the FUN3D output for time-correlated post-processing are greatly appreciated.

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